

Statistics

Fall 2022

Lecture 11



Feb 19-8:47 AM

Class QZ 11

Consider a geometric Prob. dist with p=.5

$$1) P(X=3) = \text{geomet pdf}(.5, 3) = \boxed{.125} \checkmark$$

$$2) P(X > 3) = P(X \geq 4) = 1 - P(X \leq 3) = 1 - \text{geomet cdf}(.5, 3) = \boxed{.125} \checkmark \checkmark$$



Nov 1-9:13 PM

College randomly selected 185 students and 6% of them were left-handed.

$$n=185 \Rightarrow x = n\hat{p} = 185(.06) = 11.1 \Rightarrow \boxed{x=12}$$

$\hat{p} = .06$ is decimal \Rightarrow Round-up

Find 99% Conf. interval for the prop. of all students that are left handed.

\rightarrow C-level: .99

$$.018 < p < .112$$

1-Prop Z Int

$$x=12$$

$$n=185$$

C-level: .99

We are 99% confident that between 2% & 11% of all students are left-handed.

$$E = \frac{.112 - .018}{2} = \boxed{.047}$$

$$\hat{p} = \frac{.112 + .018}{2} = \boxed{.065}$$

Point-estimate

Nov 8-6:53 PM

I randomly selected 32 nurses and their mean age was 41.5 Yrs.

$$n=32$$

$$\bar{x}=41.5$$

It is known that standard deviation of ages of all nurses is 8.6 Yrs.

$$\sigma = 8.6$$

Find Conf. interval for the mean age of all nurses

$$\boxed{38.5 < \mu < 44.5}$$

\rightarrow No C-level

\Rightarrow use .95

We are 95% confident that the mean age of all nurses is between 38.5 & 44.5 Yrs

Stats

If σ known \Rightarrow Z Interval \rightarrow Inpt:

If σ unknown \Rightarrow T Interval

$$\sigma = 8.6$$

$$\bar{x} = 41.5 \leftarrow \text{Point-estimate}$$

$$n = 32$$

C-level: .95

$$E = \frac{44.5 - 38.5}{2} = \boxed{3}$$

$$\bar{x} = \frac{44.5 + 38.5}{2} = \boxed{41.5}$$

Nov 8-7:01 PM

20 randomly selected exams had a mean of 85 and standard deviation of 10.
 $n=20$, $\bar{x}=85$, $S=10$

Find 98% Conf. interval for the mean of all exams.

C-level: .98

$$79.322 < \mu < 90.678$$

$$79 < \mu < 91$$

σ known \Rightarrow Z Interval

σ unknown \Rightarrow T Interval \Rightarrow Inpt: STATS

$$E = \frac{91 - 79}{2} = 6$$

$\bar{x}=85$ \leftarrow Point-estimate

$S=10$

$n=20$ \leftarrow $df = n-1 = 19$

C-level: .98

$$\bar{x} = \frac{91 + 79}{2} = 85$$

Nov 8-7:10 PM

I randomly selected 12 students, here are their ages:

28	18	30	42
25	20	32	38
19	50	24	36

Find

$$\bar{x} = 30.2$$

$$S = 9.9$$

$$n = 12$$

} Round to 1-decimal

Find Conf. interval for the mean age of all students.

\rightarrow NO C-level \Rightarrow Use .95

$$23.91 < \mu < 36.49$$

$$23.9 < \mu < 36.5$$

σ known \Rightarrow Z Interval

σ unknown \Rightarrow T Interval

Inpt:

Stats

$\bar{x}=30.2$ \leftarrow Point-estimate

$S=9.9$

$n=12$ \leftarrow $df = n-1 = 11$

C-level: .95

$$E = \frac{36.5 - 23.9}{2} = 6.3$$

$$\bar{x} = \frac{36.5 + 23.9}{2} = 30.2$$

Nov 8-7:18 PM

How to determine minimum Sample Size when constructing Conf. interval:

1) Working with Proportion

$$E = Z_{\alpha/2} \cdot \sqrt{\frac{\hat{p}\hat{q}}{n}} \Rightarrow \text{with some algebra work}$$

$$n = \hat{p}\hat{q} \left(\frac{Z_{\alpha/2}}{E} \right)^2$$

If decimal \Rightarrow Round-up

If \hat{p} & \hat{q} are unknown,

use .5 for each $n = .25 \left(\frac{Z_{\alpha/2}}{E} \right)^2$

2) Working with mean

$$E = Z_{\alpha/2} \cdot \frac{\sigma}{\sqrt{n}} \Rightarrow \text{with some algebra work}$$

$$n = \left(\frac{Z_{\alpha/2} \cdot \sigma}{E} \right)^2$$

If decimal \Rightarrow round-up

If σ is unknown

use S instead of σ $n = \left(\frac{Z_{\alpha/2} \cdot S}{E} \right)^2$

Nov 8-7:28 PM

Find minimum Sample Size needed if we wish to construct 90% Conf. interval for Pop. proportion with margin of error not to exceed 4% and

1) $\hat{p} = .7$

$\hat{q} = 1 - \hat{p} = .3$



$$n = \hat{p}\hat{q} \left(\frac{Z_{\alpha/2}}{E} \right)^2$$

$$= (.7)(.3) \left(\frac{1.645}{.04} \right)^2$$

$$= 355.1657 \dots$$

$Z_{.05} = \text{invNorm}(.95, 0, 1) = 1.645$

$n = 356$

2) \hat{p} & \hat{q} unknown

$$n = .25 \left(\frac{Z_{\alpha/2}}{E} \right)^2$$


$$= .25 \left(\frac{1.645}{.04} \right)^2$$

$$= 422.816 \dots$$

$n = 423$

Nov 8-7:37 PM

Find **min. Sample Size** needed to Construct **99% Conf. interval** for Pop. **mean** if we wish the margin of **error not to exceed 8** and **Standard deviation of all is 15**.

$$n = \left(\frac{Z_{\alpha/2} \cdot \sigma}{E} \right)^2 = \left(\frac{2.576 \cdot 15}{8} \right)^2 = 23.3289$$



$n = 24$

$$Z_{.005} = \text{invNorm}(.995, 0, 1) = 2.576$$

Nov 8-7:44 PM

Standard deviation of scores of randomly selected exam was 12. $S = 12$

Find **min. Sample Size** needed if we wish to construct **98% Conf. interval** for the **mean** of all exams and **error not to exceed 5**. If σ unknown, use S

$$n = \left(\frac{Z_{\alpha/2} \cdot \sigma}{E} \right)^2 \quad n = \left(\frac{Z_{\alpha/2} \cdot S}{E} \right)^2 = \left(\frac{2.326 \cdot 12}{5} \right)^2 = 31.163$$


$$Z_{.01} = \text{invNorm}(.99, 0, 1) = 2.326 \quad n = 32$$

SG 22 & SG 23

Exam II: If Your work is not similar to my notes \Rightarrow I consider it cheating.

Final Submission \Rightarrow One file, Pages in order, Portrait style, PDF or JPG file.

Hand-writing exams
No need to write the actual Problem
Page-Per-Page contents
Answers in designated area.

Nov 8-7:50 PM